# Topology-Related Modeling and Characterization of Wireless Sensor Networks PE-WASUN'2011

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Introduction

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#### Stochastic Point Process

- A stochastic point process is a probability law that describes the location of a number of points in a region of the space
- The most common model used in WSN simulation is the binomial, i.e., a fixed number of n points obeys a binomial distribution on  $W=[0,\ell]^2\subset\mathbb{R}^2$
- 2n independent identically distributed random variables  $X_1, \ldots, X_n, Y_1, \ldots, Y_n$ , obeying the uniform law on  $[0, \ell]$ , say  $x_1, \ldots, x_n, y_1, \ldots, y_n$ , and then placing the n points on coordinates  $(x_i, y_i)_{1 \le i \le n}$



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### Poisson Point Process

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 $M^2P^2$ 

$$\mathsf{M}^2\mathsf{P}^2(m,n,a,r_c,r_{ch},r_i)$$
 on  $W\subset\mathbb{R}^2$ 

It is a compounded process consisting of:

- m samples of:  $H(m, 2r_i)$  (H-sensors).
  - n-m samples of  $\Lambda(n-m,a,h)$  (L-sensors)



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# H-sensors Deployment Model

 $H(m, 2r_i)$ 

It places the maximum number of m H-sensors on a window Wrepulsed by an inhibition distance  $2r_i$ . This process follows the SSI (Simple Sequential Inhibition) stochastic point process



$$\Lambda(n-m,a,\mathbf{h})$$

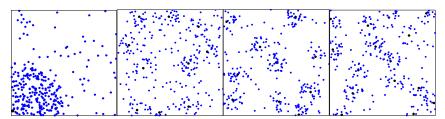
An inhomogeneous Poisson process with intensity function defined as:

$$\lambda(x,y) = \begin{cases} a, \text{if } d((x,y),(hx_i,hy_i)) \leq r_c, 1 \leq i \leq m, \\ 1, \text{ otherwise} \end{cases}$$

where a > 1 (the attractiveness parameter), d is any distance measure, and  $r_c$  is the communication radius of the L-sensors



# Examples of $M^2P^2$



Outcomes of  ${\rm M^2P^2}$  for 300 nodes with  $1,\,10,\,10$  and 15 H-sensors (in black) and attractiveness 15, 5, 15 and 15



#### Small-world characterization and energy hole behavior

- H-sensors have a two-channel radio
- Each sensor reports its collected data by using a minimum cost
- An error- and a collision-free MAC protocol was used to isolate its



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Parameter	Value
sink node	1 (center-most node)
network size	$n \in \{1000, 1500, 2000\}$ nodes
communication radius (L-sensors)	50 m
communication radius (H-sensors)	$r_{ch} \in \! \{100, 300, 500\}  \mathrm{m}$
number of H-sensors	$m \in \! \{1, 10, 30, 50\}  \mathrm{nodes}$
deployment model parameter	$a \in \{0, 1, 5, 15, 30\}$
event duration	1000s
data rate	$1\mathrm{packet/min}$
sensing radius	$30\mathrm{m}$
sensor field	$1000\times1000\mathrm{m}^2$



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- 2 independent | repulsive (a=1): binomial deployment for L-sensors and repulsive deployment for H-sensors

- strongly attractive | repulsive (a = 30): strongly attractive



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- fairly attractive | repulsive (a = 15): fairly attractive deployment
- strongly attractive | repulsive (a = 30): strongly attractive

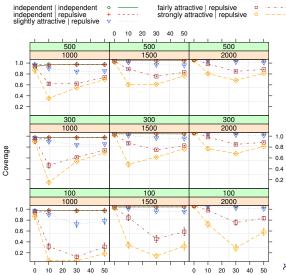


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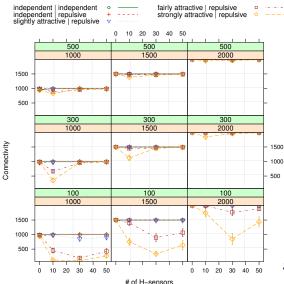




# of H-sensors



# Coverage and Connectivity





#### Small World Effect

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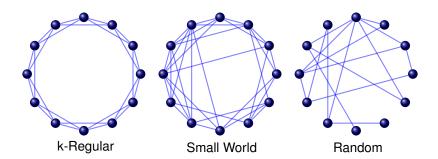


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### Small World Effect





### Small world characterization

Topology	$\overline{CC}$	$\widehat{\sigma}_{CC}$	$\overline{L}$	$\widehat{\sigma}_L$
slightly attractive   repulsive	0.658	0.009	6.313	0.553
independent   independent	0.584	0.005	8.205	0.901
homogeneous network	0.595	0.007	13.878	0.194
Erdös-Rényi random graph	0.011	0.001	2.848	0.006

1500 nodes. In the first two topologies, there are 30 H-sensors and  $r_{ch} = 300$ 



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- Betweenness appears as the metric that best describes the relay task



Evaluation of  ${\rm M}^2{\rm P}^2$ 

#### **Definitions**

Betweenness

$$B_v = \sum_{s=1}^n \sum_{t=1}^n \frac{\sigma_{st}(v)}{\sigma_{st}},$$

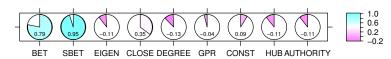
Sink-Betweenness

$$SB_v = \sum_{t=1}^n \frac{\sigma_{s_k t}(v)}{\sigma_{s_k t}}.$$



# Network Centrality and Transmitted Messages

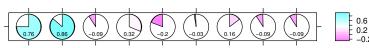
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#### Sink in a corner:



#### Sink randomly placed:



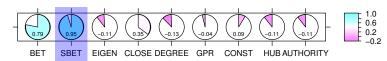
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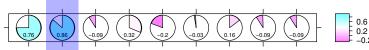
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- ullet Window W where the process takes place
- Communication radii should be carefully specified as a function of
- Number (n) and type of sensors required for precise, lasting and
- Inhibition parameter  $r_i$ ,  $r_i > r_c$  (areas of influence of H-sensors
- Intensity parameter a > 1
- L-Sensors around each H-Sensor:  $E(Z) = \frac{n-m}{m\left(\frac{1}{a}\left(\frac{\mu(W)}{\mu(W')}-1\right)+1\right)}$



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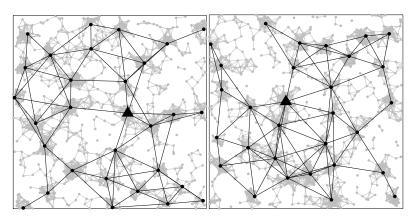


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## Two outcomes of network graphs generated by the M<sup>2</sup>P<sup>2</sup> model



1000 nodes, 30 H-sensors,  $1000 \times 1000$  sensor field,  $r_c = 50$ ,  $r_{ch} = 300$  and a = 5. E(Z) = 19.6 L-sensors.





- We showed a novel modeling solution able to represent a wide variety of WSNs scenarios
- The common random deployment is a particular case of our
- This model represents WSNs and HSNs showing characteristics
- We only need about 3% of H-sensors (50 out of 1500) to obtain
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   COPPORT

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